

21. We introduce the notion of density (which the students have probably seen in other courses):

$$\rho = \frac{m}{V}$$

and convert to SI units: $1 \text{ g} = 1 \times 10^{-3} \text{ kg}$.

- (a) For volume conversion, we find $1 \text{ cm}^3 = (1 \times 10^{-2} \text{ m})^3 = 1 \times 10^{-6} \text{ m}^3$. Thus, the density in kg/m^3 is

$$1 \text{ g}/\text{cm}^3 = \left(\frac{1 \text{ g}}{\text{cm}^3} \right) \left(\frac{10^{-3} \text{ kg}}{\text{g}} \right) \left(\frac{\text{cm}^3}{10^{-6} \text{ m}^3} \right) = 1 \times 10^3 \text{ kg}/\text{m}^3 .$$

Thus, the mass of a cubic meter of water is 1000 kg.

- (b) We divide the mass of the water by the time taken to drain it. The mass is found from $M = \rho V$ (the product of the volume of water and its density):

$$M = (5700 \text{ m}^3)(1 \times 10^3 \text{ kg}/\text{m}^3) = 5.70 \times 10^6 \text{ kg} .$$

The time is $t = (10 \text{ h})(3600 \text{ s}/\text{h}) = 3.6 \times 10^4 \text{ s}$, so the *mass flow rate* R is

$$R = \frac{M}{t} = \frac{5.70 \times 10^6 \text{ kg}}{3.6 \times 10^4 \text{ s}} = 158 \text{ kg}/\text{s} .$$