

66. (a) Ignoring air friction amounts to assuming that the ball has the same speed  $v$  when it returns to its original height.

$$K_i = K_f = \frac{1}{2}mv^2 = \frac{1}{2}(0.050\text{ kg})(16\text{ m/s})^2 = 6.4\text{ J} .$$

- (b) The momentum at the moment it is thrown (taking  $+y$  upward) is

$$|\vec{p}_i| = |\vec{p}_f| = mv = (0.050\text{ kg})(16\text{ m/s}) = 0.80\text{ kg}\cdot\text{m/s} .$$

The vector  $\vec{p}_i$  is  $\theta = 30^\circ$  above the horizontal, while  $\vec{p}_f$  is  $30^\circ$  below the horizontal (since the vertical component is now downward). We note for later reference that the magnitude of the change in momentum is

$$|\Delta\vec{p}| = |\vec{p}_f - \vec{p}_i| = 2mv \sin \theta = 0.80\text{ kg}\cdot\text{m/s}$$

and  $\Delta\vec{p}$  points vertically downward.

- (c) The time of flight for the ball is  $t = 2v_i \sin \theta / g$ , thus

$$mgt = mg \left( \frac{2v \sin \theta}{g} \right) = 2mv \sin \theta = 2p_i \sin \theta = 0.80\text{ kg}\cdot\text{m/s}$$

which (recalling our result in part (b)) illustrates the relation  $|\Delta p| = Ft$  where  $F = mg$ .