

56. (a) By a force analysis in the style of Chapter 6, we find the normal force $N = mg \cos \theta$ (where $mg = 267 \text{ N}$) which means $f_k = \mu_k mg \cos \theta$. Thus, Eq. 8-29 yields

$$\Delta E_{\text{th}} = f_k d = \mu_k mg d \cos \theta = (0.10)(267)(6.1) \cos 20^\circ = 1.5 \times 10^2 \text{ J} .$$

- (b) The potential energy change is $\Delta U = mg(-d \sin \theta) = (267)(-6.1 \sin 20^\circ) = -5.6 \times 10^2 \text{ J}$. The initial kinetic energy is

$$K_i = \frac{1}{2} m v_i^2 = \frac{1}{2} \left(\frac{267 \text{ N}}{9.8 \text{ m/s}^2} \right) (0.457 \text{ m/s})^2 = 2.8 \text{ J} .$$

Therefore, using Eq. 8-31 (with $W = 0$), the final kinetic energy is

$$K_f = K_i - \Delta U - \Delta E_{\text{th}} = 2.8 - (-5.6 \times 10^2) - 1.5 \times 10^2 = 4.1 \times 10^2 \text{ J} .$$

Consequently, the final speed is $v_f = \sqrt{2K_f/m} = 5.5 \text{ m/s}$