

48. The direction of motion (the direction of the barge's acceleration) is $+\hat{i}$, and $+\hat{j}$ is chosen so that the pull \vec{F}_h from the horse is in the first quadrant. The components of the unknown force of the water are denoted simply F_x and F_y .

(a) Newton's second law applied to the barge, in the x and y directions, leads to

$$\begin{aligned}(7900 \text{ N}) \cos 18^\circ + F_x &= ma \\ (7900 \text{ N}) \sin 18^\circ + F_y &= 0\end{aligned}$$

respectively. Plugging in $a = 0.12 \text{ m/s}^2$ and $m = 9500 \text{ kg}$, we obtain $F_x = 6.4 \times 10^3 \text{ N}$ and $F_y = -2.4 \times 10^3 \text{ N}$. The magnitude of the force of the water is therefore

$$F_{\text{water}} = \sqrt{F_x^2 + F_y^2} = 6.8 \times 10^3 \text{ N}.$$

(b) Its angle measured from $+\hat{i}$ is either

$$\tan^{-1} \left(\frac{F_y}{F_x} \right) = -21^\circ \quad \text{or} \quad 159^\circ.$$

The signs of the components indicate the former is correct, so \vec{F}_{water} is at 21° measured clockwise from the line of motion.