

13. We take $t = 0$ at the start of the interval and take the sense of rotation as positive. Then at the end of the $t = 4.0\text{ s}$ interval, the angular displacement is $\theta = \omega_0 t + \frac{1}{2}\alpha t^2$. We solve for the angular velocity at the start of the interval:

$$\omega_0 = \frac{\theta - \frac{1}{2}\alpha t^2}{t} = \frac{120\text{ rad} - \frac{1}{2}(3.0\text{ rad/s}^2)(4.0\text{ s})^2}{4.0\text{ s}} = 24\text{ rad/s} .$$

We now use $\omega = \omega_0 + \alpha t$ (Eq. 11-12) to find the time when the wheel is at rest:

$$t = -\frac{\omega_0}{\alpha} = -\frac{24\text{ rad/s}}{3.0\text{ rad/s}^2} = -8.0\text{ s} .$$

That is, the wheel started from rest 8.0 s before the start of the described 4.0 s interval.