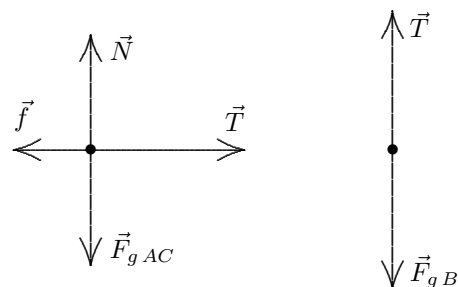


15. (a) Free-body diagrams for the blocks  $A$  and  $C$ , considered as a single object, and for the block  $B$  are shown below.  $T$  is the magnitude of the tension force of the rope,  $N$  is the magnitude of the normal force of the table on block  $A$ ,  $f$  is the magnitude of the force of friction,  $W_{AC}$  is the combined weight of blocks  $A$  and  $C$  (the magnitude of force  $\vec{F}_{gAC}$  shown in the figure), and  $W_B$  is the weight of block  $B$  (the magnitude of force  $\vec{F}_{gB}$  shown). Assume the blocks are not moving. For the blocks on the table we take the  $x$  axis to be to the right and the  $y$  axis to be upward. The  $x$  component of Newton's second law is then  $T - f = 0$  and the  $y$  component is  $N - W_{AC} = 0$ . For block  $B$  take the downward direction to be positive. Then Newton's second law for that block is  $W_B - T = 0$ . The third equation gives  $T = W_B$  and the first gives  $f = T = W_B$ . The second equation gives  $N = W_{AC}$ . If sliding is not to occur,  $f$  must be less than  $\mu_s N$ , or  $W_B < \mu_s W_{AC}$ . The smallest that  $W_{AC}$  can be with the blocks still at rest is  $W_{AC} = W_B / \mu_s = (22 \text{ N}) / (0.20) = 110 \text{ N}$ . Since the weight of block  $A$  is  $44 \text{ N}$ , the least weight for  $C$  is  $110 - 44 = 66 \text{ N}$ .



- (b) The second law equations become  $T - f = (W_A/g)a$ ,  $N - W_A = 0$ , and  $W_B - T = (W_B/g)a$ . In addition,  $f = \mu_k N$ . The second equation gives  $N = W_A$ , so  $f = \mu_k W_A$ . The third gives  $T = W_B - (W_B/g)a$ . Substituting these two expressions into the first equation, we obtain  $W_B - (W_B/g)a - \mu_k W_A = (W_A/g)a$ . Therefore,

$$a = \frac{g(W_B - \mu_k W_A)}{W_A + W_B} = \frac{(9.8 \text{ m/s}^2)(22 \text{ N} - (0.15)(44 \text{ N}))}{44 \text{ N} + 22 \text{ N}} = 2.3 \text{ m/s}^2.$$