

75. We choose  $\hat{i}$  East and  $\hat{j}$  North, and use SI units. The ball initially moving eastward has mass  $m_1 = 5.0$  kg and initial velocity  $\vec{v}_{1i} = 4.0\hat{i}$  m/s, and the ball initially moving westward has mass  $m_2 = 4.0$  kg and velocity  $\vec{v}_{2i} = -3.0\hat{i}$  m/s. The final velocity of  $m_1$  is  $\vec{v}_{1f} = -1.2\hat{j}$ .

(a) Momentum conservation leads to

$$\begin{aligned} m_1\vec{v}_{1i} + m_2\vec{v}_{2i} &= m_1\vec{v}_1 + m_2\vec{v}_2 \\ 20\hat{i} - 12\hat{i} &= -6\hat{j} + 4\vec{v}_2 \end{aligned}$$

which leads to

$$\vec{v}_2 = 2.0\hat{i} + 1.5\hat{j} \implies v_2 = (2.5 \angle 37^\circ)$$

where magnitude-angle notation is used. Thus, the speed of the 4.0 kg ball just after the collision is 2.5 m/s.

(b) We compute the decrease in total kinetic energy:

$$K_i - K_f = \frac{1}{2}(5)(4)^2 + \frac{1}{2}(4)(3)^2 - \frac{1}{2}(5)(1.2)^2 - \frac{1}{2}(4)(2.5)^2$$

which gives the result 42 J.