

103. We choose *down* as the  $+y$  direction and place the coordinate origin at the top of the building (which has height  $H$ ). During its fall, the ball passes (with velocity  $v_1$ ) the top of the window (which is at  $y_1$ ) at time  $t_1$ , and passes the bottom (which is at  $y_2$ ) at time  $t_2$ . We are told  $y_2 - y_1 = 1.20$  m and  $t_2 - t_1 = 0.125$  s. Using Eq. 2-15 we have

$$y_2 - y_1 = v_1 (t_2 - t_1) + \frac{1}{2}g (t_2 - t_1)^2$$

which immediately yields

$$v_1 = \frac{1.20 - \frac{1}{2}(9.8)(0.125)^2}{0.125} = 8.99 \text{ m/s} .$$

From this, Eq. 2-16 (with  $v_0 = 0$ ) reveals the value of  $y_1$ :

$$v_1^2 = 2gy_1 \implies y_1 = \frac{8.99^2}{2(9.8)} = 4.12 \text{ m} .$$

It reaches the ground ( $y_3 = H$ ) at  $t_3$ . Because of the symmetry expressed in the problem (“upward flight is a reverse of the fall”) we know that  $t_3 - t_2 = 2.00/2 = 1.00$  s. And this means  $t_3 - t_1 = 1.00 + 0.125 = 1.125$  s. Now Eq. 2-15 produces

$$\begin{aligned} y_3 - y_1 &= v_1 (t_3 - t_1) + \frac{1}{2}g (t_3 - t_1)^2 \\ y_3 - 4.12 &= (8.99)(1.125) + \frac{1}{2}(9.8)(1.125)^2 \end{aligned}$$

which yields  $y_3 = H = 20.4$  m.