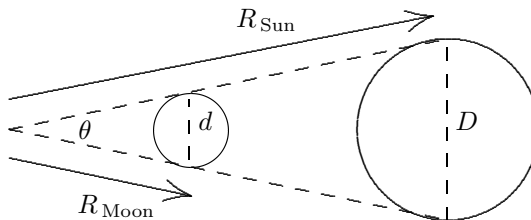


35. (a) When  $\theta$  is measured in radians, it is equal to the arclength divided by the radius. For very large radius circles and small values of  $\theta$ , such as we deal with in this problem, the arcs may be approximated as straight lines – which for our purposes correspond to the diameters  $d$  and  $D$  of the Moon and Sun, respectively. Thus,



$$\theta = \frac{d}{R_{\text{Moon}}} = \frac{D}{R_{\text{Sun}}} \implies \frac{R_{\text{Sun}}}{R_{\text{Moon}}} = \frac{D}{d}$$

which yields  $D/d = 400$ .

- (b) Various geometric formulas are given in Appendix E. Using  $r_s$  and  $r_m$  for the radius of the Sun and Moon, respectively (noting that their ratio is the same as  $D/d$ ), then the Sun's volume divided by that of the Moon is

$$\frac{\frac{4}{3}\pi r_s^3}{\frac{4}{3}\pi r_m^3} = \left(\frac{r_s}{r_m}\right)^3 = 400^3 = 6.4 \times 10^7 .$$

- (c) The angle should turn out to be roughly 0.009 rad (or about half a degree). Putting this into the equation above, we get

$$d = \theta R_{\text{Moon}} = (0.009) (3.8 \times 10^5) \approx 3.4 \times 10^3 \text{ km} .$$