

7. We denote the two forces \vec{F}_1 and \vec{F}_2 . According to Newton's second law, $\vec{F}_1 + \vec{F}_2 = m\vec{a}$, so $\vec{F}_2 = m\vec{a} - \vec{F}_1$.

(a) In unit vector notation $\vec{F}_1 = (20.0 \text{ N})\hat{i}$ and

$$\vec{a} = -(12 \sin 30^\circ \text{ m/s}^2)\hat{i} - (12 \cos 30^\circ \text{ m/s}^2)\hat{j} = -(6.0 \text{ m/s}^2)\hat{i} - (10.4 \text{ m/s}^2)\hat{j} .$$

Therefore,

$$\begin{aligned}\vec{F}_2 &= (2.0 \text{ kg}) \left(-6.0 \text{ m/s}^2 \right) \hat{i} + (2.0 \text{ kg}) \left(-10.4 \text{ m/s}^2 \right) \hat{j} - (20.0 \text{ N})\hat{i} \\ &= (-32 \text{ N})\hat{i} - (21 \text{ N})\hat{j} .\end{aligned}$$

(b) The magnitude of \vec{F}_2 is

$$\left| \vec{F}_2 \right| = \sqrt{F_{2x}^2 + F_{2y}^2} = \sqrt{(-32)^2 + (-21)^2} = 38 \text{ N} .$$

(c) The angle that \vec{F}_2 makes with the positive x axis is found from $\tan \theta = F_{2y}/F_{2x} = 21/32 = 0.656$. Consequently, the angle is either 33° or $33^\circ + 180^\circ = 213^\circ$. Since both the x and y components are negative, the correct result is 213° .