

68. (a) The effect of a (sliding) friction is described in terms of energy dissipated as shown in Eq. 8-29. We have

$$\Delta E = K + \frac{1}{2}k(0.08)^2 - \frac{1}{2}k(0.10)^2 = -f_k(0.02)$$

where distances are in meters and energies are in Joules. With  $k = 4000$  N/m and  $f_k = 80$  N, we obtain  $K = 5.6$  J.

- (b) In this case, we have  $d = 0.10$  m. Thus,

$$\Delta E = K + 0 - \frac{1}{2}k(0.10)^2 = -f_k(0.10)$$

which leads to  $K = 12$  J.

- (c) We can approach this two ways. One way is to examine the dependence of energy on the variable  $d$ :

$$\Delta E = K + \frac{1}{2}k(d_0 - d)^2 - \frac{1}{2}kd_0^2 = -f_k d$$

where  $d_0 = 0.10$  m, and solving for  $K$  as a function of  $d$ :

$$K = -\frac{1}{2}kd^2 + (kd_0)d - f_k d .$$

In this first approach, we could work through the  $\frac{dK}{dd} = 0$  condition (or with the special capabilities of a graphing calculator) to obtain the answer  $K_{\max} = \frac{1}{2k}(kd_0 - f_k)^2$ . In the second (and perhaps easier) approach, we note that  $K$  is maximum where  $v$  is maximum – which is where  $a = 0 \implies$  equilibrium of forces. Thus, the second approach simply solves for the equilibrium position

$$|F_{\text{spring}}| = f_k \implies kx = 80 .$$

Thus, with  $k = 4000$  N/m we obtain  $x = 0.02$  m. But  $x = d_0 - d$  so this corresponds to  $d = 0.08$  m. Then the methods of part (a) lead to the answer  $K_{\max} = 12.8 \approx 13$  J.