

8. On the one hand, we could perform the vector addition of the displacements with a vector capable calculator in polar mode  $((75 \angle 37^\circ) + (65 \angle -90^\circ) = (63 \angle -18^\circ))$ , but in keeping with Eq. 3-5 and Eq. 3-6 we will show the details in unit-vector notation. We use a ‘standard’ coordinate system with  $+x$  East and  $+y$  North. Lengths are in kilometers and times are in hours.

- (a) We perform the vector addition of individual displacements to find the net displacement of the camel.

$$\begin{aligned}\Delta\vec{r}_1 &= 75\cos(37^\circ)\hat{i} + 75\sin(37^\circ)\hat{j} \\ \Delta\vec{r}_2 &= -65\hat{j} \\ \Delta\vec{r}_1 + \Delta\vec{r}_2 &= 60\hat{i} - 20\hat{j} \text{ km} .\end{aligned}$$

If it is desired to express this in magnitude-angle notation, then this is equivalent to a vector of length  $\sqrt{60^2 + (-20)^2} = 63 \text{ km}$ , which is directed at  $18^\circ$  south of east.

- (b) We use the result from part (a) in Eq. 4-8 along with the fact that  $\Delta t = 90 \text{ h}$ . In unit vector notation, we obtain

$$\vec{v}_{\text{avg}} = \frac{60\hat{i} - 20\hat{j}}{90} = 0.66\hat{i} - 0.22\hat{j}$$

in kilometers-per-hour. This result in magnitude-angle notation is  $\vec{v}_{\text{avg}} = 0.70 \text{ km/h}$  at  $18^\circ$  south of east.

- (c) Average speed is distinguished from the magnitude of average velocity in that it depends on the total distance as opposed to the net displacement. Since the camel travels  $140 \text{ km}$ , we obtain  $140/90 = 1.56 \text{ km/h}$ .
- (d) The net displacement is required to be the  $90 \text{ km}$  East from  $A$  to  $B$ . The displacement from the resting place to  $B$  is denoted  $\vec{r}_3$ . Thus, we must have (in kilometers)

$$\vec{r}_1 + \vec{r}_2 + \vec{r}_3 = 90\hat{i}$$

which produces  $\vec{r}_3 = 30\hat{i} + 20\hat{j}$  in unit-vector notation, or  $(36 \angle 33^\circ)$  in magnitude-angle notation. Therefore, using Eq. 4-8 we obtain

$$|\vec{v}_{\text{avg}}| = \frac{36 \text{ km}}{120 - 90 \text{ h}} = 1.2 \text{ km/h}$$

and the direction of this vector is the same as  $\vec{r}_3$  (that is,  $33^\circ$  north of east).