

12. (a) The mass of each spherical hailstone of radius  $r = 0.5$  cm and density  $\rho = 0.92$  g/cm<sup>3</sup> is

$$m = \rho \left( \frac{4\pi r^3}{3} \right) = 0.48 \text{ g} = 4.8 \times 10^{-4} \text{ kg} .$$

- (b) If the final speed is zero, then Eq. 10-4 and Eq. 10-8 (with  $+y$  upward) lead to

$$\vec{F}_{\text{avg}} \Delta t = -m\vec{v}_i = - (4.8 \times 10^{-4}) (-25) = 0.012$$

in SI units (N·s). This gives the impulse imparted to a single hailstone by the roof (and is equal to the magnitude of the force on the roof by the hailstone, by Newton's third law). An imagined "cube" of falling air,  $\ell = 1$  m on each side (falling with the hail at  $v = 25$  m/s), takes a time of

$$\Delta t = \frac{\ell}{v} = \frac{1 \text{ m}}{25 \text{ m/s}} = 0.04 \text{ s}$$

to fully "collapse" onto a square meter of roof top (delivering its load of 120 hailstones). We can cover an area of  $10 \text{ m} \times 20 \text{ m}$  with 200 of these "collapsing cubes" of air. Therefore, in this time, the total impulse is of magnitude

$$\vec{F}_{\text{avg, total}} \Delta t = 200(120)(0.012 \text{ N}\cdot\text{s}) \approx 290 \text{ N}\cdot\text{s}$$

which leads to  $\vec{F}_{\text{avg, total}} = 290/0.04 = 7.2 \times 10^3 \text{ N}$ .