

109. (Fifth problem of **Cluster 1**)

The problem consists of two parts, where part 1 ( $A$  to  $B$ ) involves constant velocity motion for  $t_1 = 5.00$  s and part 2 ( $B$  to  $C$ ) involves uniformly accelerated motion. Assuming the coordinate origin is at point  $A$  and the positive axis is directed towards  $B$  and  $C$ , then we have  $x_C = 250$  m,  $a_2 = -0.500$  m/s<sup>2</sup>, and  $v_C = 0$ .

- (a) We set up the uniform velocity equation for part 1 ( $\Delta x = vt$ ) and Eq. 2-16 for part 2 ( $v^2 = v_0^2 + 2a\Delta x$ ) as a simultaneous set of equations to be solved:

$$\begin{aligned} x_B - 0 &= v_1(5.00) \\ 0^2 &= v_B^2 + 2(-0.500)(250 - x_B) . \end{aligned}$$

Bearing in mind that  $v_A = v_1 = v_B$ , we can solve the equations by, for instance, substituting the first into the second – eliminating  $x_B$  and leading to a quadratic equation for  $v_1$ :

$$v_1^2 + 5v_1 - 150 = 0 .$$

The positive root gives us  $v_1 = 13.5$  m/s.

- (b) We obtain the duration  $t_2$  of part 2 from Eq. 2-11:

$$v = v_0 + at_2 \implies 0 = 13.5 + (-0.500)t_2$$

which yields the value  $t_2 = 27.0$  s. Therefore, the total time is  $t_1 + t_2 = 32.0$  s.